

AP Calculus

3.4/18 $f(x) = \frac{(x^2+1) \cdot \cot x}{3 - \cos x \csc x}$

$(x^2+1)(\cot x)$
is a product
is it the whole thing?

$$g(x) = (x^2+1)$$

$$h(x) = \frac{\cot x}{3 - \cos x \csc x}$$

$$(gh)' = g'h + gh'$$

$$* = (2x) \left(\frac{\cot x}{3 - \cos x \csc x} \right) + (x^2+1) \left(\frac{\cot x}{3 - \cos x \csc x} \right)'$$

$$1 \quad \frac{d}{dx} \left(\frac{\cot x}{3 - \cos x \csc x} \right) = \frac{(-\csc^2 x)(3 - \cos x \csc x) - (\cot x)(-(-\csc^2 x))}{(3 - \cos x \csc x)^2}$$

$$\frac{d}{dx} \left(\frac{f}{g} \right) = \frac{f'g - fg'}{g^2}$$

$$\frac{d}{dx} (\cos x \csc x) = \frac{d}{dx} \left(\cos x \left(\frac{1}{\sin x} \right) \right) \quad \left[\cot x = \frac{\cos x}{\sin x} \right]$$

$$* = \frac{2x \cot x}{3 - \cos x \csc x} + \frac{(x^2+1)(-3\csc^2 x + \cos x \csc^3 x - \cot x \csc^2 x)}{(3 - \cos x \csc x)^2}$$

$$f(x) = \frac{(x^2+1) \cot x}{3 - \cos x \csc x}$$

$$f(x) = \frac{g(x)}{h(x)}$$

$$\frac{([2x][\cot x] + [x^2+1][-\csc^2 x])(3 - \cos x \csc x) - (x^2+1)(\cot x)(\csc^2 x)}{(3 - \cos x \csc x)^2}$$

$$\left(\frac{g}{h}\right)' = \frac{g'h - gh'}{h^2}$$

$$f(x) = \frac{(x^2+1) \cdot \cot x}{3 - \cos x \csc x}$$

$$f(x) = \frac{\left[(x^2+1) \left(\frac{\cos x}{\sin x} \right) \right] \sin x}{\left[3 - \frac{\cos x}{\sin x} \right] \sin x}$$

$$\left(\frac{f}{g} \right)' = \frac{f'g - fg'}{g^2}$$

$$f(x) = \frac{(x^2+1)(\cos x)}{3\sin x - \cos x}$$

$$f'(x) = \frac{\left[(2x)(\cos x) + (x^2+1)(-\sin x) \right] (3\sin x - \cos x) - (x^2+1)(\cos x)(3\cos x + \sin x)}{(3\sin x - \cos x)^2}$$

3.3
17

$$f(x) = \frac{g(x) \cdot (\sin x \sec x)}{h(x) = (1 + x \tan x)}$$

$$f'(x) = \frac{(\sec^2 x)(1 + x \tan x) - \tan x(\tan x + x \sec^2 x)}{(1 + x \tan x)^2}$$

$$= \frac{\sec^2 x + x \sec^2 x \tan x - \tan^2 x - x \tan x \sec^2 x}{(1 + x \tan x)^2}$$

$$= \frac{\sec^2 x - \tan^2 x}{(1 + x \tan x)^2}$$

$\sin x \sec x = \sin x \left(\frac{1}{\cos x} \right) = \frac{\sin x}{\cos x} = \tan x$
 $\frac{d}{dx}(x \tan x) = (1) \tan x + (x)(\sec^2 x)$
 $\frac{\sin^2 + \cos^2}{\cos^2} = 1$
 $\frac{\tan^2 x + 1}{1 - \tan^2 x} = \sec^2 x$
 $1 = \sec^2 x - \tan^2 x$

CALCULUS LOOKS at TRIG

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$$

$$\frac{d}{dx}(\sin x) = \cos x \quad \frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x \quad \frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x \quad \frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\lim_{x \rightarrow 0} \left(\frac{1 - \cos x}{x} \right) \left(\frac{1 + \cos x}{1 + \cos x} \right) =$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos^2 x}{x(1 + \cos x)} = \lim_{x \rightarrow 0} \frac{\sin^2 x}{x(1 + \cos x)}$$

$$\lim_{x \rightarrow 0} \left(\frac{\sin x}{x} \right) \left(\frac{\sin x}{1 + \cos x} \right) = 0$$

Algebra looks at trig

2.6/p 163/41

$$f(x) = \begin{cases} \frac{\tan(kx)}{x}, & x < 0 \\ 3x + 2k^2, & x \geq 0 \end{cases}$$

$$\lim_{x \rightarrow 0^-} \frac{\tan(kx)}{x}$$

$$= \lim_{x \rightarrow 0^-} \frac{\sin(kx)}{x} \left(\frac{1}{\cos(kx)} \right)$$

$$= \lim_{x \rightarrow 0^-} k \left(\frac{\sin(kx)}{kx} \right) \left(\frac{1}{\cos(kx)} \right)$$

$$= k(1)(1) = k$$

$$\lim_{x \rightarrow 0^+} 3x + 2k^2$$

$$= 2k^2$$

$$k = 2k^2$$

$$k - 2k^2 = 0$$

$$k(1 - 2k) = 0$$

$$k = 0$$

$$k = \frac{1}{2}$$

$$\cancel{k = 0}$$

for $k = \frac{1}{2}$,
is function
continuous?